

## Warm Up

1) Expand the following:

a)  $\log \underline{4} \cdot \underline{x^3} \cdot \underline{y^4}$

$\log 4 + 3 \log x + 4 \log y$

b)  $\log 2 \frac{x^2 y}{z^3}$

$\log 2 + 2 \log x + \log y - 3 \log z$

2) Condense the following:

a)  $\log_3 4 + 3 \log_3 x$

$\log_3 4 \cdot x^3$

b)  $4 \log_4 2 - \log_4 5$

$\log_4 \frac{2^4}{5}$

3) Use the change of base:

a)  $\log_4 7$

$\frac{\log 7}{\log 4}$

b)  $\log_5 13$

\*calculator trick

## Homework Questions

$$\begin{array}{l} \textcircled{27} \log_2 \sqrt{x} \\ \swarrow \log_2 x^{\frac{1}{2}} \\ \frac{1}{2} \log_2 x \end{array}$$

$$\begin{array}{l} \textcircled{29} \ln \sqrt[4]{x^3} \\ \ln x^{3/4} \\ \frac{3}{4} \ln x \end{array}$$

$$\textcircled{41}$$

\*Activity- Math Lib

\* "Where would you find a prehistoric cow?" ws

$$\log_3 6 + 2 \cdot \log_3 x + \frac{1}{2} \log_3 9$$

$$\log_3 6 \cdot x^2 \cdot 3$$

$$\log_3 18x^2$$

## 7.6 Solving Exponential and Logarithmic Equations

- \*What does it mean to be a solution?
- \*Why do extraneous solutions exist?
- \*What are the appropriate operations to solving exponential & logarithmic equations?

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## 7.6 Solving Exponential and Logarithmic Equations

### Property of Equality for Exponential Equations

\*If  $b$  is a positive number other than 1, then  $b^x = b^y$  if and only if  $x = y$ .

Example:

If  $3^x = 3^5$ , then  $x = 5$ . If  $x = 5$ , then  $3^x = 3^5$ .



Examples:

$$A) 9^{2x} = 27^{x-1}$$

$$\cancel{3}^{2(2x)} = \cancel{3}^{3(x-1)}$$

$$4x = 3x - 3$$

$$-3x \quad -3x$$

$$1x = -3$$

$$C) \cancel{8}^{2x} = \cancel{8}^{x+7}$$

$$2x = x + 7$$

$$x = 7$$

$$B) \cancel{3}^{-3x+1} = \cancel{3}^{x-9}$$

$$-3x+1 = x-9$$

$$-x \quad - \quad -x \quad -$$

$$-4x = -10$$

$$\frac{-4x}{-4} = \frac{-10}{-4}$$

$$x = \frac{5}{2}$$

$$D) 8^{x-1} = \left(\frac{1}{2}\right)^{2x-1}$$

$$\left(\frac{1}{2}\right)^{-3(x-1)} = \left(\frac{1}{2}\right)^{2x-1}$$

$$-3(x-1) = 2x-1$$

$$-3x+3 = 2x-1$$

$$-5x = -4$$

$$x = \frac{4}{5}$$

How do I solve equations with e?

$$1) e^x = 1$$

$$x = \ln(1)$$

$$x = 0$$

$$2) e^{x+1} = 7$$

$$\ln e^{x+1} = \ln 7$$

$$x + 1 = \ln(7)$$

$$x = 1.79$$

$$3) \left(\frac{3}{4}\right)e^{3x-8} = -6$$

$$\frac{3}{4} \cdot \frac{3}{4} e^{3x-8} = 2 \cdot \frac{3}{4}$$

$$\ln e^{3x-8} = \ln \left(\frac{2 \cdot 3}{3}\right)$$

$$\frac{3x-8}{3} = \ln \left(\frac{2 \cdot 3}{3}\right)$$

$$x = \frac{\ln \left(\frac{2 \cdot 3}{3}\right) + 8}{3}$$

How do I solve equations with ln?

$$1) -2 + \ln 2x = 1$$

$$\begin{aligned} & \overset{+2}{e^{\ln 2x}} = \overset{+2}{e^3} \\ & 2x = \frac{e^3}{2} \\ & x = \frac{e^3}{4} \end{aligned}$$

$$2) \ln 2x + \ln 4x = 2$$

$$\begin{aligned} & \ln 2x \cdot 4x = 2 \\ & e^{\ln(8x^2)} = e^2 \\ & 8x^2 = \frac{e^2}{8} \\ & \sqrt{x^2} = \sqrt{\frac{e^2}{64}} \\ & x = \sqrt{\frac{e^2}{64}} \\ & x = .96 \end{aligned}$$

\*Natural Logarithms Equations Maze

## Points

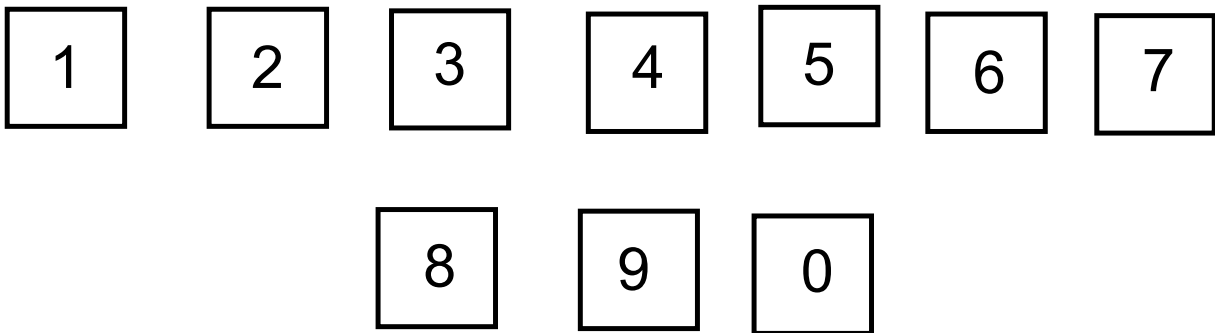
1 point for each addition used in an equation

2 points for each subtraction used in an equation

3 points for each multiplication used in an equation

4 points for each division used in an equation

Can you make it?



Can you make



using-

## 7.6 Solving Exponential and Logarithmic Equations

### Property of Equality for Logarithmic Equations

\*If  $b$ ,  $x$ , and  $y$  are positive numbers with  $b \neq 1$ , then  $\log_b x = \log_b y$  if and only if  $x = y$ .

Example:

If  $\log_2 x = \log_2 7$ , then  $x = 7$ .

If  $x = 7$ , then  $\log_2 x = \log_2 7$ .

$$1) \log_7(2-x) = \log_7 5x$$

$$\begin{array}{r} 2-x = 5x \\ +x \quad +x \end{array}$$

$$\frac{2}{6} = \frac{6x}{6}$$

$$\frac{1}{3} = x$$

$$2) \frac{2 \log_7(1-2x)}{2} = \frac{12}{2}$$

$$\log_7(1-2x) = 6$$

$$7^6 = 1-2x$$

$$117649 = 1-2x$$

$$\frac{117648}{-2} = \frac{-2x}{-2}$$

$$x = -58824$$



3)  $\log_3 x = 5$

$$3^5 = x$$

$$x = 243$$

$$\boxed{3^{4x} = 27}$$

$$\log_3 27 = 4x$$

$$\frac{3}{4} = \frac{4x}{4}$$

$$\frac{\log 27}{\log 3} = x$$

4)  $3^{4x} = 27$

$$B^{4x} = B^3$$

$$\frac{4x}{4} = \frac{3}{4}$$

$$x = \frac{3}{4}$$

\* "If you had eight porcupines in on hand and seven porcupines in the other, what would you have?" WS

# Homework:

★Page 519#3-42 multiples of 3, 55, 56b &c, 57,  
58

★ WS's (finish)

## Reminders

\*Review packet due and Test on

Red- 18th

Blue- 22nd